

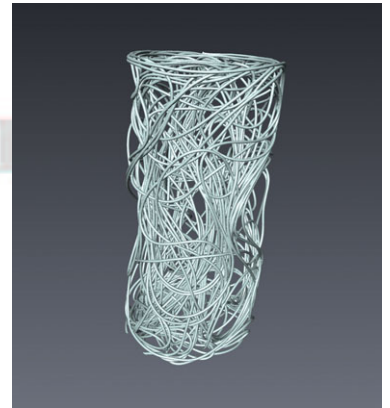
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Mechanical Properties of Monofilament Entangled Materials

L. Courtois, E. Maire, M. Perez, D. Rodney, O. Bouaziz, Y. Brechet*

Monofilament entangled materials are a new type of materials with promising mechanical properties. They are made of a single wire randomly packed into a finite volume whose dimensions are much larger than the wire length, thus providing many self-contacts. Their complex internal architecture is investigated using X-ray tomography in order to link the microstructural evolution to the mechanical behaviour. This material exhibits very interesting properties in terms of vibration damping.

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Mechanical Properties of Monofilament Entangled Materials**

By Loïc Courtois,* Eric Maire, Michel Perez, David Rodney, Olivier Bouaziz and Yves Brechet

Monofilament entangled materials are a new type of materials with promising mechanical properties. They are made of a single wire randomly packed into a finite volume whose dimensions are much larger than the wire length, thus providing many self-contacts. Their complex internal architecture is investigated using X-ray tomography. The evolution of the number of contacts per unit volume, as well as of the density profiles, is monitored during a compression test in order to link the microstructural evolution of the sample to its mechanical behavior. This material exhibits very interesting properties in terms of vibration damping.

1 Playing with the architecture of a material is a promising
2 way of tailoring its properties for multifunctional applica-
3 tions. What is now referred to as “architected materials”
4 (metal foams,^[1] entangled materials,^[2] steel wool,^[3] etc.), has
5 triggered numerous research in recent years, mostly for their
6 ability to be engineered in order to exhibit specific combina-
7 tions of properties, which “classical materials” could not offer.
8 These materials have been proposed as ideal candidates for a
9 top-down approach of “materials by design.” In this context,
10 some studies have been carried out concerning entangled
11 materials,^[4] but only a few on monofilament entangled
12 materials.^[5–7] Such a material, with no filament ends, sliding

contacts and a high relative porosity (80–95%), could exhibit 1
interesting properties for shock absorption, vibration damp- 2
ing and ductility. The simplicity of the manufacturing process 3
as well as the large permeability and the resistance to high and 4
low temperatures, are also of interest for high technology 5
applications, such as high strength seals or vibration damping 6
materials. 7

Because of the complex architecture of these materials, 8
X-ray tomography is used in this paper as a main 9
characterization method. This technique enables a 3D 10
nondestructive microstructural characterization of the mate- 11
rial,^[3] which can be coupled with an in situ mechanical 12
characterization. Different parameters can be measured from 13
the acquired 3D data (density profiles, number of contact per 14
unit of volume, and volume fractions) and linked to the global 15
mechanical behavior. 16

The purpose of this study is to investigate the compressive 17
properties and the damping abilities of monofilament 18
entangled materials for different wire diameters, volume 19
fractions, and initial geometries of the wire.^[8] Both the 20
microstructural analysis and the mechanical analysis will 21
provide information on the behavior of this architected 22
material. 23

1. Experimental Procedure and Results 24

1.1. Fabrication of the Steel Wire Entanglement 25

Steel wires were used in this study as a raw material. Their 26
dimensions, as well as their mechanical properties are listed in 27
Table 1. 28

The wire was first entangled manually to form a precursory 29
wire-bundle. This bundle was then placed into a specific PTFE 30
cylindrical die with a 15 mm diameter. The samples were 31
initially 35 mm high with a 5% volume fraction. The control of 32

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of the tomography scans. In addition, we would like to thank
Dr. S. Meille and P. Clement for their help with the execution of
the dynamic mechanical analysis.

Table 1. Properties of the used wires.

Material	Diameters [μm]	Yield strength [MPa]
Stainless steel 304L	127, 200, and 280	200
Pearlitic steel	120	4000

distribution along the compression axis (z-axis). By measuring, for each cross-section of the sample (perpendicular to the z-direction), the ratio of the number of white pixels over the total number of pixels constitutive of the sample, we could measure a local density value, at a given z position (from top to bottom: 0–1). We could also measure the mean local orientation of the wire of the studied cross-section as a function of z. The aspect ratio of the cross-section of each intersection between the wire and the slice located at z provided information about the local orientation of the wire. Indeed, the cross-section of a perfectly vertical part of the wire appears as a circle whereas that of a segment perpendicular to the compression axis appears as a very elongated ellipse.

Figure 2 shows, for example, the evolution of the density and orientation distribution along the compression axis for a sample made of a stainless steel wire with a 200 μm diameter. We can notice a relatively homogeneous profile in the initial state (5%, figures on the left), except for the denser parts at the top and bottom of the sample (this “wall effect” will be discussed later in this paper). In terms of orientation, the internal part of the sample seems to be composed of wire sections oriented at an average angle of 35° whereas close to both ends, the wire tends to be oriented parallel to the horizontal faces of the mold.

With the increase of the volume fraction, densification peaks start to appear and grow (Figure 2d). From the orientation distribution along the compression axis (z-direction), we can clearly see that densification is accompanied by a reorientation of the wire in the direction perpendicular to the compression axis (highest angle between the z-axis and the wire). This structuring in the z-direction shows that the deformation of this material is not homogeneous and that localized deformation is accompanied by local densification and fiber reorientation.

To fully characterize the microstructure, it is also possible to study the density distribution along the radial direction. A local density was measured at a given r distance from the axis of the cylindrical die, averaged over the total height of the sample. By doing so for each position between the center (radial position = 0) and the side of the mold, a radial density

1 the volume fraction was achieved through the measurement
2 of the total length of the wire.

3 Once inside the mold, the samples were submitted to a
4 constrained compressive test up to a final volume fraction of
5 17.5%. In this study, the compression state of the sample was
6 characterized by its volume fraction, which appeared to be the
7 most relevant parameter.

8 1.2. *In situ X-ray Microtomography*

9 In order to fully characterize the complex internal
10 architecture of this material, an in situ compressive test was
11 set up within the tomograph (Figure 1a). The cylindrical die,
12 coupled to a piston rod, was placed inside a dedicated
13 compressive machine, shown in Figure 1b,^[9] which was fixed
14 on the turntable of the tomograph.

15 The samples were compressed, step by step, and for each
16 step, samples were unloaded. From the displacement of the
17 grips and the initial length and diameter of the wires, it was
18 possible to calculate the “theoretical” volume fraction of the
19 sample during compression tests (starting at 5%). A 3D
20 volume was acquired and reconstructed from a set of X-ray
21 scans (Figure 1b). Each radiograph was acquired with a 24 μm
22 voxel size.

23 1.3. *Microstructural Characterization*

24 In order to link the internal architecture to the global
25 mechanical strength of the samples, a microstructural analysis
26 was performed based on the 3D images. These were first
27 processed to obtain a binary image where the wire appeared
28 as white voxels, and the air as black. The homogeneity of the
29 sample was studied by monitoring the evolution of the density

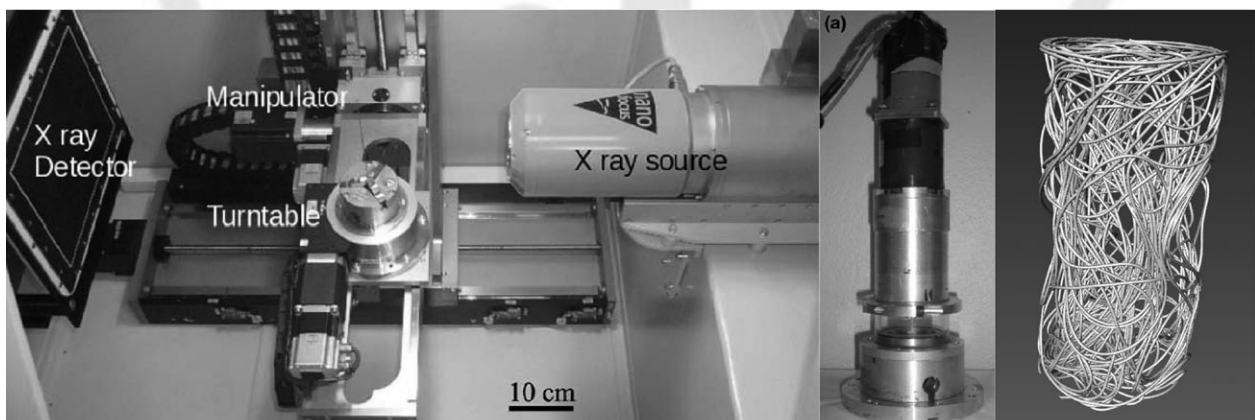


Fig. 1. (a) Internal chamber of the used tomograph, (b) in situ experimental compressive device, (c) example of a reconstructed 3D volume (diameter of the sample: 15 mm).

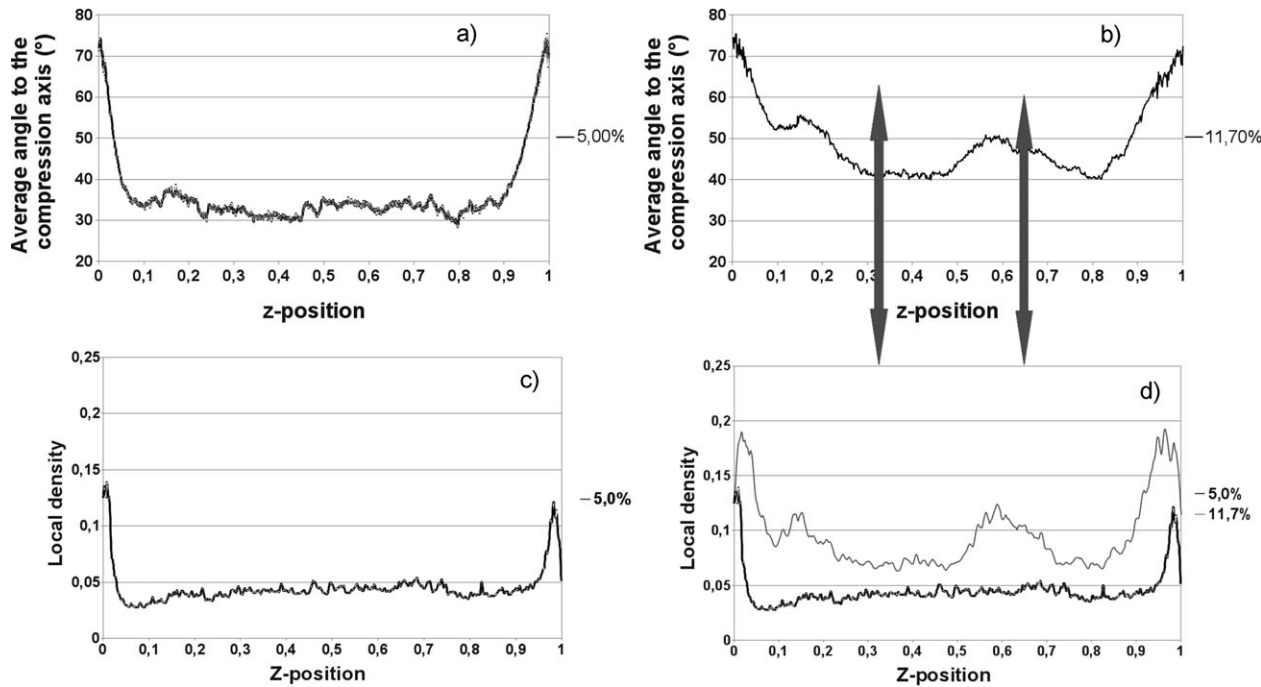


Fig. 2. (a–d) Evolution of the orientation (a and b) and local density (c and d) along the compression axis for two different densities (5%, figures a and c and 11.7% figures b and d).

1 profile could be measured. Figure 3a shows the influence of
 2 the diameter of the initial stainless steel wire used to produce
 3 the entanglement on the radial density profile. We can first
 4 notice a heterogeneous distribution of the wire with a higher

local density close to the contact with the mold. This “wall 1
 effect” is typical of confined entangled media and seems to be 2
 less important for a smaller diameter of the wire. This was 3
 expected since a smaller wire diameter means a smaller 4
 bending modulus and thus more flexibility of the wire and 5
 easier arrangements for the same mold radius. 6

From the experiment with the pearlitic steel, we could 7
 study the influence of the yield strength of the wire on the 8
 density distribution. From the radial density profiles shown in 9
 Figure 3a, it can clearly be seen that the density gradient in 10
 case of high yield strength (pearlitic steel) is much more 11
 important than for low yield strength (stainless steel). This 12
 strong heterogeneity might also play a role on the mechanical 13
 response of this material. We have, locally, a very dense 14
 material which will tend to rigidify the structure. 15

Figure 3b presents the evolution of the normalized radial 16
 density profile (local density divided by the height of the 17
 sample) with the volume fraction, for a sample made of a 18
 200 μm stainless steel wire. We can notice that the general 19
 shape of the profile does not evolve much. This would indicate 20
 that there is no re-arrangement of the wire in the radial 21
 direction when compressing the entanglement. The material is 22
 compressed along the compression axis with no evolution of 23
 the radial distribution. 24

From the binary 3D images, it was possible to measure the 25
 number of contacts per unit of volume. The data was first 26
 reduced to its center-line (skeletonization of the wire 27
 architecture). The whole structure then consisted in a list of 28
 segments and nodes where one contact corresponded to an 29
 H-like structure. By counting the number of segments shorter 30
 than the diameter of the wire (definition of a contact point), we 31

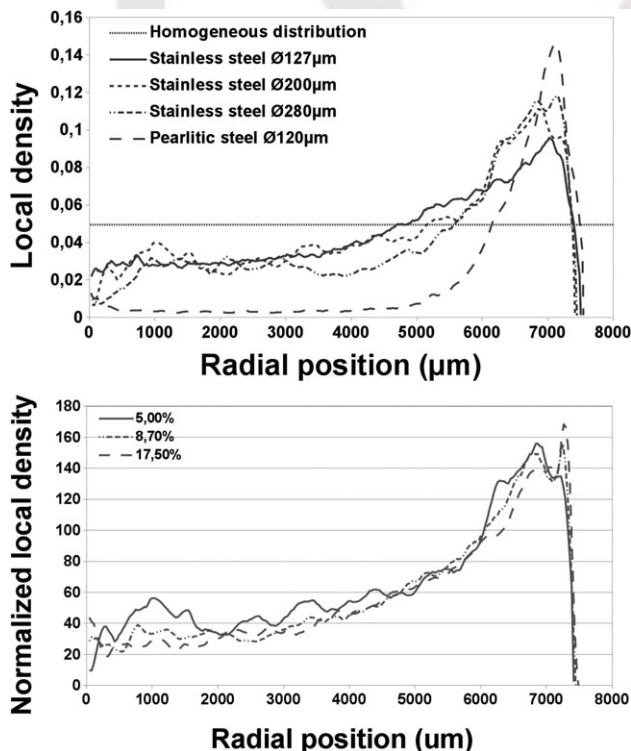


Fig. 3. (a) Influence of the diameter and yield strength on the radial density profiles. (b) Evolution of the radial density profile with the volume fraction.

1 could estimate the number of contacts per unit volume. This
2 evaluation could be refined with the extra assumption that, if
3 the distance between two short segments is smaller than the
4 diameter of the wire, those two segments belong to the same
5 contact point.

6 In this specific architected structure, the mechanical
7 strength mostly comes from the creation of contact points
8 through the compression. Thus, from the tomography data,
9 the evolution of the number of contacts per unit volume was
10 studied. These experimental values can be compared to a
11 model proposed by Toll which yields the following relation-
12 ship between the number of contacts per unit of volume N_{cv}
13 and the relative density ρ .^[10]

$$N_{cv} = \frac{16f}{\pi^2 d_f^3} \rho^2 \quad (1)$$

14 where d_f is the diameter of the fiber and f is a parameter
15 describing the fiber orientation distribution.

16 In the case of a sample made of a stainless steel
17 wire, Figure 4 shows the evolution of the experimental
18 and predicted number of contacts per unit volume with
19 the volume fraction and wire diameter for the whole
20 sample. We can see at first that, just as the model
21 predicts, the number of contacts evolves as a function of
22 the square of the volume fraction. Indeed, the slopes of the
23 experimental results are almost identical to the one of the
24 model in this log–log plot. This evolution tends to prove that
25 the mechanical strength of this material will increase with the
26 volume fraction. We can also notice that the contact density
27 decreases with the diameter of the wire. This was expected
28 since, for a smaller diameter, the length of the wire gets longer,
29 for a given volume fraction. As a result, more contacts
30 are created.

31 Although the general slope of the experimental plot does fit
32 the model, the absolute values are not in agreement with the
33 model. One reason might be that, since we are using the same
34 resolution for all diameters, the contacts might not be as well
35 defined for thin wires as for thicker ones. Additionally, some
36 hypothesis of the model might not be fulfilled in the
37

experiment. For example, the model assumes a random
isotropic distribution of fiber orientations in an infinite
system, whereas we have seen that there are strong
heterogeneities near the walls and the fibers have a
preferential orientation.

From those measurements, it was possible to link the
evolution of the internal microstructure to the mechanical
behavior of this material and thus, have a better under-
standing of the behavior of the entangled media under
compressive loading.

1.4. Mechanical Characterization

The samples were compressed with a strain rate of
 $5 \times 10^{-4} \text{ s}^{-1}$. During the whole in situ compression test, a
stress–strain curve was acquired. In this study, the stress
values were plotted as a function of the volume fraction,
which appeared to be more relevant for this type of entangled
material.

For each compression step, corresponding to known
volume fractions (6, 7, 8.7, 11.7, and 17.5%), the samples
were unloaded and the strength of the entanglement was
characterized by discharge modulus measurements (slope of
the stress–strain curve at the first instant of the discharge).
After unloading, the sample was reloaded in order to observe
the hysteresis phenomenon.

As commonly observed in entangled materials,^[11] the
compressive mechanical behavior of the entanglement shows
a nonlinear evolution (Figure 5a). There is no regime in which
a purely linear elastic deformation could be observed. The
material gets more and more dense as the number of contacts
per unit volume increases, and the wire is deformed by
bending between two contact points. We can also notice a very
strong hysteresis phenomenon when a cyclic load is applied
(unloading/reloading). This means that this material does
indeed exhibit good damping abilities.

The stiffness of the material was assessed by measurements
of the slope at the very first beginning of the unloading
sequence (see Figure 5a). The stiffness of this material ranges
from 20 to 200 MPa over the studied volume fraction range.
Figure 5b shows that the entanglement tends to become stiffer
as the volume fraction increases. We can also notice that, even
though it was shown that for a smaller wire diameter, the
contact density was higher, the samples tend to be less stiff.
Therefore, there seems to be a compromise between the
number of contacts per unit of volume and the wire stiffness,
which decreases with the diameter. A higher yield strength of
the wire seems (if the diameter is constant) to increase the
rigidity of the sample. Indeed, the mechanical behavior of the
sample made of a pearlitic wire is very close to the one made of
a stainless steel wire with a diameter more than twice larger
(Figure 5a), although the elastic moduli of the constitutive
materials are very similar. This higher mechanical response
for a higher yield strength might come from the very
heterogeneous density distribution that was previously shown
but also from the higher mechanical properties of the wire
itself. Furthermore, the deformation, in the case of the pearlitic

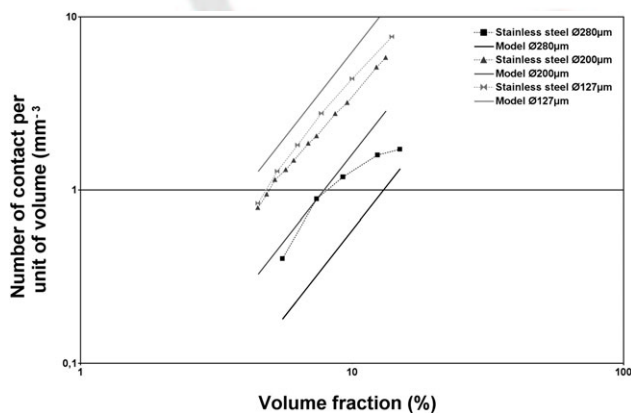


Fig. 4. Evolution of the number of contacts per unit of volume with the volume fraction.

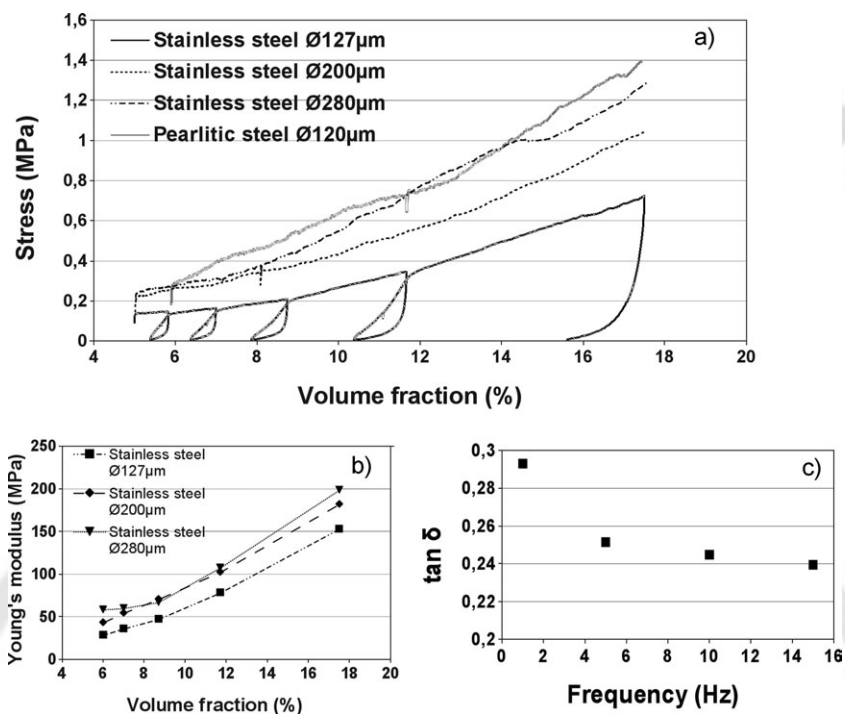


Fig. 5. (a) $\text{Stress} = f(\text{volume fraction})$, (b) evolution of the Young's modulus with the volume fraction, (c) evolution of the loss factor with the frequency for a 200 μm stainless steel wire.

1 steel wire, is almost entirely elastic whereas it is mostly plastic
2 for stainless steel wires.

3 In parallel, a dynamic mechanical analysis was performed
4 on a BOSE Electroforce 3200. The samples were shaped
5 inside the cylindrical PTFE mold and then taken out of it in
6 order to place them in-between two compression plates.
7 This procedure was selected to perform a measurement of
8 the damping of the entanglement alone avoiding the effect of
9 the mold. A sinusoidal displacement (0.3 mm amplitude)
10 was imposed on a stainless steel sample (200 μm diameter)
11 with a 10% volume fraction, submitted to a 5 N preload, and
12 the resulting force was acquired. The phase angle difference
13 (δ) between those two signals (force and displacement)
14 was computed, from which the loss factor ($\tan \delta$) was
15 deduced. This $\tan \delta$ value is an indicator of the capacity of
16 the material to absorb energy. In this particular case, it is
17 thought to be mostly through friction at contact points
18 between wire segments.

19 Since the measurements were not constrained (no
20 cylindrical die), only the stainless steel wire samples were
21 analyzed. Indeed, the samples made of a pearlitic steel
22 wire did not stay in shape when taken out of the containing
23 mold.

24 This analysis was performed in order to estimate the loss
25 factor of this material and to study the influence of the
26 frequency on its ability to absorb energy. A mean $\tan \delta$ of 0.25
27 was observed, which is quite high if we consider that the one
28 of polyurethane is around 0.5. Figure 5c) shows a decrease of
29 the loss factor with the frequency. This would indicate that the
30 energy dissipation mechanisms, mostly friction, are more
31 efficient at low frequency.

2. Conclusion

1
2 The behavior of a steel entanglement was studied under a 2
3 compressive load. Experiments were performed in situ with 3
4 tomography and enabled a complete microstructural char- 4
5 acterization of the very complex architecture of the material. 5

6 This monofilament entangled material was shown to be 6
7 very heterogeneous with a very strong "wall effect" that could 7
8 be reduced by using smaller wire diameters. The evolution of 8
9 the number of contacts per unit of volume was studied and 9
10 compared to a model for entangled media. The experiment 10
11 showed an overall good agreement with the model. We were 11
12 also able to relate the local orientation state to the density 12
13 distribution inside the sample. 13

14 The stiffness of this material was shown to be in a 14
15 20–200 MPa range, which is relatively high for a highly porous 15
16 entangled material. It is also worth noticing that the entangled 16
17 structure, under a compressive load, exhibits a stiffness 17
18 evolution, with the volume fraction, opposite to many usual 18
19 cellular materials (foams, e.g., tend to get weaker when 19
20 compressed). Its damping ability was also investigated and a 20
21 dynamic mechanical analysis underlined its great capacity to 21
22 absorb energy, with a loss factor of about 0.25. 22

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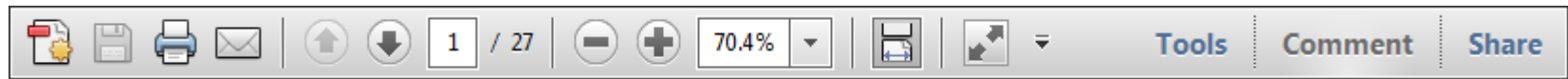
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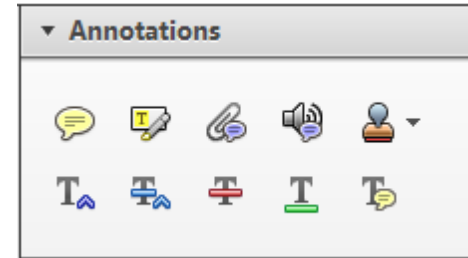
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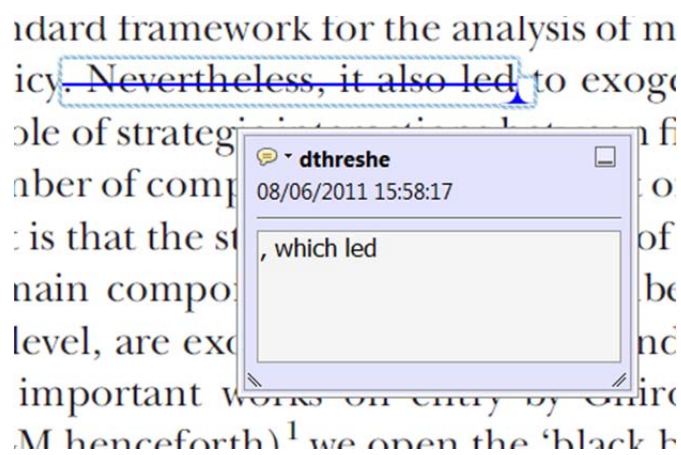
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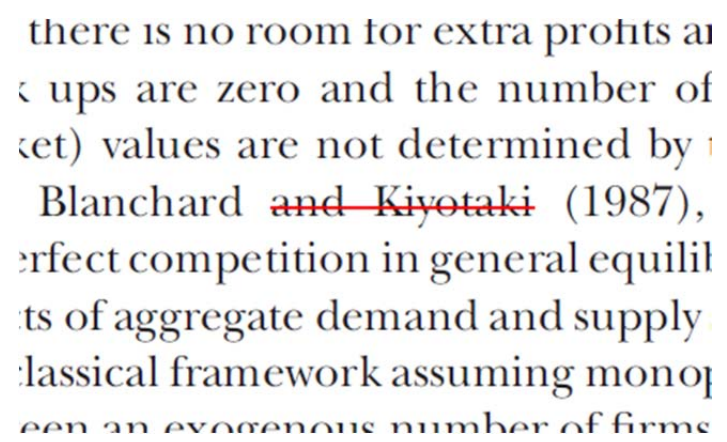
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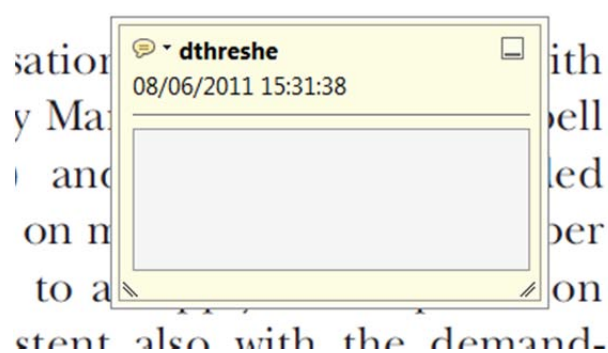
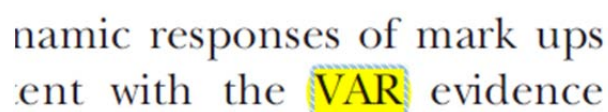
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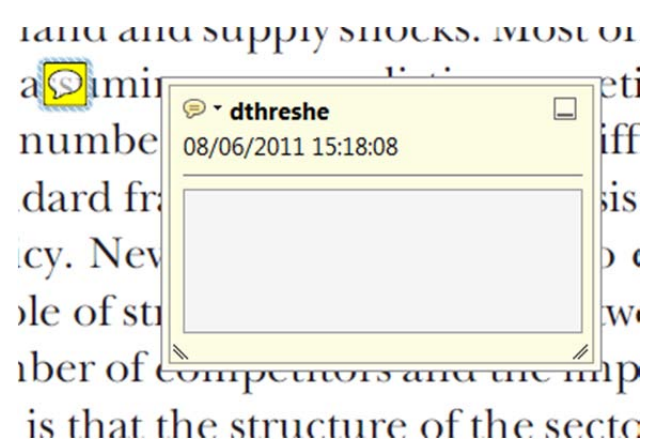
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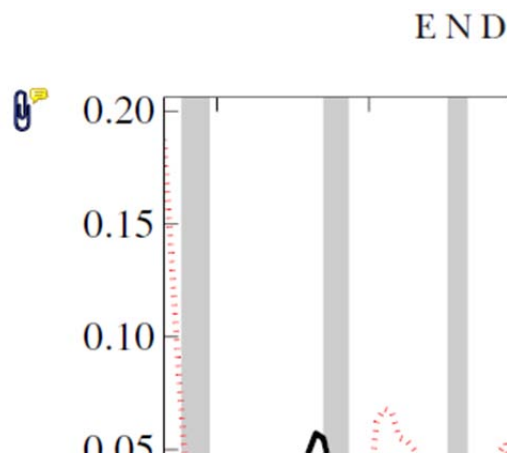
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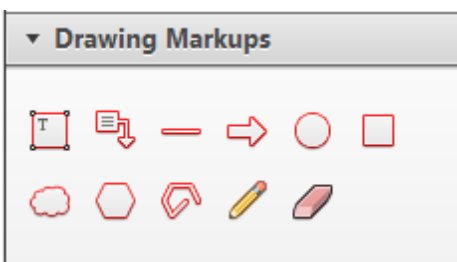


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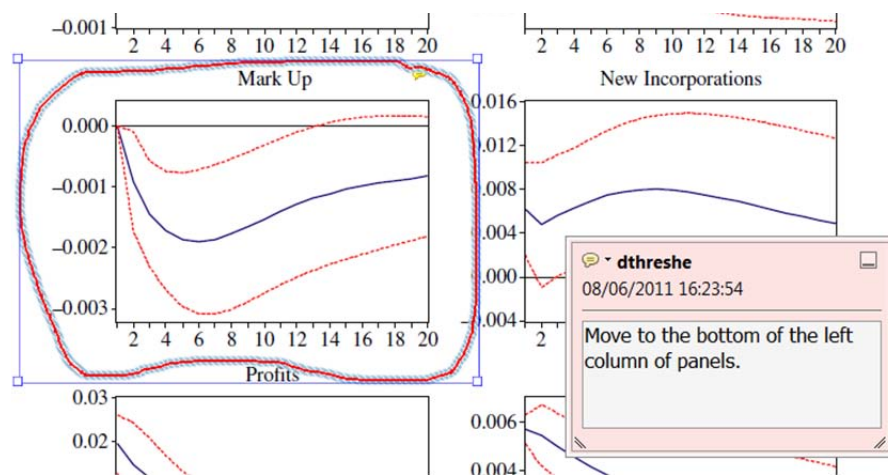


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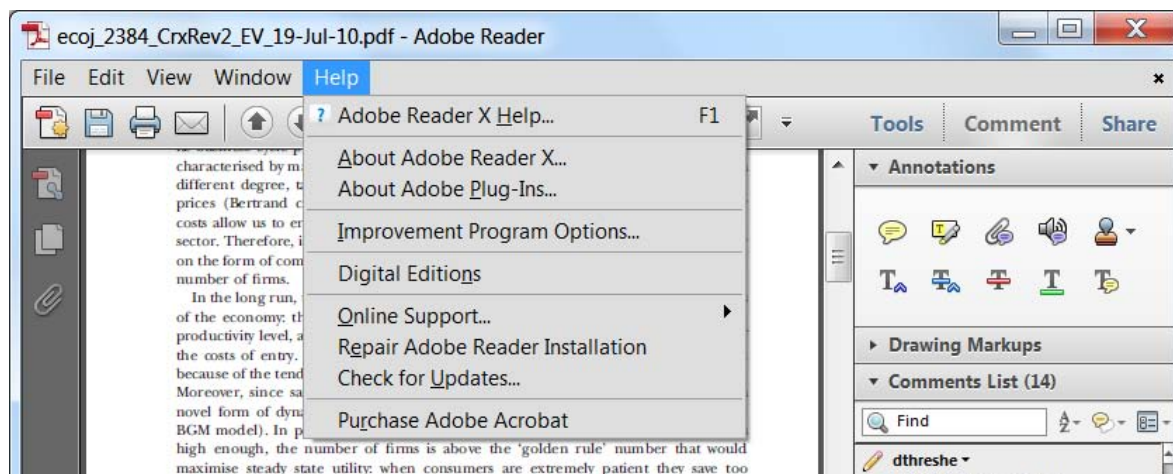
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